Electrochemical compressor driven metal hydride heat pump

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ABSTRACT

In this study, a new metal hydride heat pump system driven by an electrochemical compressor was proposed. The system uses the electrochemical compressor to generate absorption heating and desorption cooling in two identical LaNi5 reactors operating at different pressure levels. A thermodynamic model was developed to predict the system performance in terms of various parameters. Modeling shows EC compression efficiency has a great impact on system performance. The system is suitable for cooling application less than 200 W where mechanical compressors are the most inefficient. The high compression efficiency of electrochemical compressor could potentially make the cooling system more competitive than existing metal hydride heat pump systems.

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Keywords:
Electrochemical compressor
Metal hydride
Heat pump
Proton exchange membrane

Pompe à chaleur en hydrure métallique entrainée par un compresseur électrochimique

Mots-clés : Compresseur électrochimique ; Hydrure métallique ; Pompe à chaleur ; Membrane d’échange de proton

1. Introduction

In the United States, heating ventilation and air conditioning (HVAC) system accounts for 41% of commercial building energy consumption and 36% of residential building energy consumption (Goetzler et al., 2014). Most of the energy consumed by the HVAC system in residential and commercial buildings is used for space heating and cooling, which is mostly based on the vapor compression cycle. Conventional vapor compression cycles use refrigerants such as R-134a and R-410A that have high global warming potential. Therefore,
solid state cooling technologies have been developed to address the global warming challenges and enhance the efficiency. Metal hydride (MH) cooling and heating technologies are developed with metals or alloys, which can absorb hydrogen reversibly to form MHs. The reaction can be described as eq. (1) (Hirscher, 2010; Sandrock, 1999).

\[
M + \frac{X}{2}H_2 \leftrightarrow MH_x + Q
\]  

where Q is the heat of reaction of hydride formation.

Absorption reaction is exothermic, while desorption reaction is endothermic, based on eq. (1). A metal can absorb or desorb hydrogen at given temperature depending on its phase equilibrium plateau pressure \(P_m\). The absorption process is shown in Fig. 1. Initially, the metal can dissolve some hydrogen atoms into its lattice to form a solid solution (α phase). When either the hydrogen concentration or the pressure increases further at a given temperature, a MH phase (β phase) starts to form. Starting at that point, a plateau is observed where both α and β phases coexist (Hirscher, 2010). The plateau is similar to the latent heat of a pure substance, such as the latent heat of evaporating water. The Van’t Hoff equation below (eq. (2)) describes the midpoint plateau pressure in relation with temperature at given enthalpy of formation and entropy of formation (Hirscher, 2010; Sandrock, 1999).

\[
\ln \left( \frac{P_m}{P_0} \right) = \frac{\Delta H}{RT} - \frac{\Delta S}{R}
\]  

where \(P_0\) is the reference pressure of 1 bar, and R is the gas constant. Under a given temperature, the metal absorbs hydrogen when the pressure is above the plateau pressure, while below the plateau pressure, the hydride (β phase) is unstable and releases hydrogen.

Nafion is widely used in fuel cells as the proton exchange membrane (Barbir, 2005; Benziger et al., 2011). EC working mechanism is shown in Fig. 2. With the help of a catalyst such as platinum, hydrogen decomposes to protons and electrons on one side of the membrane (anode) and then protons travel across the membrane. Whereas electrons take a different route, driven by an external voltage to the other side (cathode) where they recombine with protons to regenerate hydrogen. As long as the driving force (voltage) is constant, hydrogen transfer across the membrane can happen at a constant rate, which can be calculated from Faraday’s Law (Rohland et al., 1998) in eq. (3).

\[
\frac{dn}{dt} = \frac{I}{2F}
\]  

where \(dn/dt\) is the hydrogen flowrate across the membrane, I is the current generated by the voltage supply, F is Faraday’s constant. If hydrogen is transferred to the cathode with a constant volume that is less than the anode, the pressure on the cathode increases and an electrochemical compressor is therefore developed. Since clean hydrogen is re-produced at the

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### Nomenclatures

<table>
<thead>
<tr>
<th>Symbols</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td>A</td>
<td>activated cell area ([cm^2])</td>
</tr>
<tr>
<td>F</td>
<td>Faraday’s constant ([c⋅mol^{-1}])</td>
</tr>
<tr>
<td>ΔH</td>
<td>enthalpy change of formation ([kJ⋅mol^{-1}])</td>
</tr>
<tr>
<td>I_d</td>
<td>current density ([A⋅cm^{-2}])</td>
</tr>
<tr>
<td>I</td>
<td>current ([A])</td>
</tr>
<tr>
<td>N</td>
<td>number of electrochemical compressors connected in parallel</td>
</tr>
<tr>
<td>P</td>
<td>pressure ([bar])</td>
</tr>
<tr>
<td>Q</td>
<td>capacity ([W])</td>
</tr>
<tr>
<td>R</td>
<td>gas constant ([J⋅mol^{-1}⋅K^{-1}])</td>
</tr>
<tr>
<td>R_i</td>
<td>internal resistance ([Ω⋅cm^2])</td>
</tr>
<tr>
<td>ΔS</td>
<td>entropy change of formation ([kJ⋅mol^{-1}⋅K^{-1}])</td>
</tr>
<tr>
<td>T</td>
<td>temperature ([°C])</td>
</tr>
<tr>
<td>U_ac</td>
<td>cathode and anode polarization ([V])</td>
</tr>
<tr>
<td>U_Nernst</td>
<td>Nernst potential ([V])</td>
</tr>
<tr>
<td>U_ohm</td>
<td>ohmic loss ([V])</td>
</tr>
<tr>
<td>W.Ed</td>
<td>power consumption ([W])</td>
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### Subscript: acronyms

| a | absorption |
| c | cooling |
| d | desorption |
| dis | discharge |
| EC | electrochemical compressor |
| eff | effectiveness |
| eq | equilibrium |
| h | heating |
| HVAC | heating ventilation and air conditioning |
| hyst | hysteresis |
| i | internal |
| in | indoor |
| m | midpoint of plateau |
| MEA | membrane electrolyte assembly |
| MH | metal hydride |
| o | reference |
| out | outdoor |
| R | reactor |
| s | surface |
| suc | suction |

---

**Fig. 1** – Pressure–composition isotherms of MH.
cathode through chemical reactions, there is very little contamination (Rohland et al., 1998; Strobel et al., 2002). Several studies have been conducted by different groups to investigate the EC performance (Gardner and Ternan, 2007; Grigoriev et al., 2011; Onda et al., 2007; Rohland et al., 1998; Sedlak et al., 1981; Strobel et al., 2002). According to the research done previously, the pressure limit of hydrogen reached by the EC from atmospheric pressure can vary from 20 bar to 1000 bar (Bouwman, 2014; Grigoriev et al., 2011; Lipp, 2012; Lipp and Patel, 2011; Rohland et al., 1998; Strobel et al., 2002). In order to achieve very high pressure, multiple stacks of ECs are required, and membranes need to be backed up with supporting material. The efficiency of EC can be around 90% at small hydrogen flowrates (Bouwman, 2014; Lipp, 2012; Lipp and Patel, 2011). The comparison of different selected ECs developed is listed in Table 1.

Because of the exothermic and endothermic behaviors of absorption and desorption processes, MH has been previously studied for heat pumps. The heat pump systems have been reviewed by different authors (Muthukumar and Groll, 2010; Takeda et al., 2009). There are mainly two ways of using MH as heat pumps: heat driven MH heat pump, and compressor driven MH heat pump (Muthukumar and Groll, 2010; Takeda et al., 2009). The heat driven MH heat pump is based on transferring hydrogen between two or more reactors, exploiting the different absorption and desorption pressures and temperatures of each reactor to generate heating or cooling (Muthukumar and Groll, 2010). As shown in Fig. 3, low temperature MH reactor A and high temperature MH reactor B are connected. Each reactor contains a different MH material. During the operation, MH reactor A releases hydrogen by taking up waste heat at low temperature. Hydrogen released flows to the other reactor which absorbs hydrogen at high temperature to generate useful space heating. The cooling process takes place when the high temperature MH reactor B is cooled by rejecting heat to the air and absorbs hydrogen, which reduces the hydrogen pressure of the system and causes low temperature MH reactor A to desorb hydrogen and generates useful space cooling. This type of the MH heat pump usually has COP less than 1 (Zhong and Glanville, 2014). The compressor driven MH heat pump usually uses two identical MH reactors (Muthukumar and Groll, 2010; Takeda et al., 2009). A mechanical compressor reduces the pressure of the desorption reactor and increases the pressure of absorption reactor (Fig. 4) (Kim et al., 1997). Thus one reactor desorbs hydrogen and generates cooling at low pressure and temperature, while the other reactor absorbs hydrogen and generates heating at high pressure and temperature. The compressor driven MH heat pump is studied by various groups using a mechanical compressor to maintain the pressure difference by driving hydrogen from one reactor to the other (Kim et al., 1997; Magnetto et al., 2006; Mazumdar et al., 2004; Park et al., 2001, 2002). Table 2 lists previous mechanical compressor driven MH heat pump developed by different groups. Kim et al. (1997) conducted steady state simulation and calculated the COP of LaNi5 system to be 4.3 for a 3.5 kW system with cooling temperature at 8 °C and heating temperature at 46 °C, however, they did not con-

<table>
<thead>
<tr>
<th>Table 1 – Electrochemical compressor compression limit.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Group</td>
</tr>
<tr>
<td>Rohland et al. (1998)</td>
</tr>
<tr>
<td>Strobel et al. (2002)</td>
</tr>
<tr>
<td>Grigoriev et al. (2011)</td>
</tr>
<tr>
<td>Lipp (2012)</td>
</tr>
<tr>
<td>Bouwman (2014)</td>
</tr>
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</table>

Fig. 2 – Working principle of EC.

Fig. 3 – Heat driven MH heat pump, using the difference of absorption and desorption pressure of different MH materials.

Fig. 4 – Mechanical compressor driven MH heat pump.
sider the hysteresis of the MH material, pressure drop during suction and discharge of hydrogen, and heat exchanger effectiveness, so their modeling results might be a bit optimistic. Park et al. (2002) conducted the experiment on Zr$_{0.9}$Ti$_{0.1}$Cr$_{0.55}$Fe$_{1.45}$ and measured the COP to be 1.8 for a 1.4 kW system with cooling temperature at 6 °C and heating temperature at 32 °C. Mazumdar et al. (2004) conducted the transient simulation using Zr$_{0.9}$Ti$_{0.1}$Cr$_{0.55}$Fe$_{1.45}$, taking into account the heat transfer and calculated the COP to be 2.5 with cooling temperature at 22 °C and heating temperature of 32 °C for a 1 kW system. Magnetto et al. (2006) developed a prototype of Mm based alloy that shows COP of 2.6 for a 2 kW system with cooling temperature at 20 °C and heating temperature at 45 °C.

The existing MH heat pump technologies have their limitations. The heat driven MH heat pump has a low COP, while the mechanical compressor efficiency limits the mechanical compressor driven MH heat pump performance. Currently, small hydrogen compressors required for small compressor driven metal hydride cooling systems with less than 200 W of cooling capacity have around 65% isentropic efficiency. Moreover, the compressed hydrogen usually contains traces of lubrication oil that potentially reduce the MH absorption and desorption performance. In order to solve all above limitations, the EC driven MH heat pump was proposed in this paper, and its system performance was investigated.

2. Process description for EC driven MH heat pump

The MH heat pump system driven by the EC is similar to the previously developed mechanical compressor driven MH heat pump as two identical MH reactors, one for cooling and one for heating, are connected by the compressors in both systems. However, in the proposed MH heat pump system, the mechanical compressor is replaced by the EC. As shown in Fig. 5, the EC is placed in between two identical LaNi$_5$ MH reactors so that one side generates cooling at low pressure and the other side produces heating at high pressure. Hydrogen is desorbed from the MH reactor, where pressure is below the plateau pressure at low system pressure and temperature of heat source. Meanwhile, hydrogen is pumped to and absorbed in the MH reactor on the other side where the pressure is above the plateau pressure at high system pressure and temperature of heat sink. LaNi$_5$ was chosen for modeling, because it is the most commonly used MH for heat pump development as pointed out from the most recent review papers (Sandrock and Bowman, 2003; Zhong and Glanville, 2014). In addition, LaNi$_5$ and its AB$_5$ hydride family absorb and desorb hydrogen in room temperature at reasonable pressure range (100–400 kPa) with small hysteresis (Hirscher, 2010; Sandrock, 1999).

The uniqueness of choosing EC to be the compressor is that the anode and cathode of the EC are both identical, which makes it possible to switch hydrogen flow direction by switching the polarity of power supply. A continuously operating system of the EC heat pump with indoor and outdoor heat exchangers is therefore proposed. As it is shown in Fig. 6, initially, the reactor on the left (bed 1) is full of hydrogen and reactor on the right (bed 2) is empty of hydrogen. After the EC is turned on, hydrogen pressure is reduced in the left reactor as desorption occurs, so that temperature drops and cooling is generated at Ts (Fig. 6a). This cold reactor is in heat exchange with the indoor heat exchanger. As pressure increases on the right reactor (bed 2), absorption occurs so that temperature increases and heating is generated at Tc. This hot reactor is in heat exchange with the outdoor heat exchanger. When bed 1 is depleted and bed 2 is full, bed 1 (cold) is pre-heated and bed 2 (hot) is pre-cooled by air at room temperature (Fig. 6b). Finally, as shown in Fig. 6c, the polarity of power supply is switched, so that hydrogen flows from bed 2 to bed 1, bed 2 therefore generates cooling and bed 1 generates heating by switching the heat transfer fluid flow of corresponding indoor and outdoor heat exchangers. The cycle operation of MH is shown on the Van’t Hoff chart (Fig. 7).

3. Thermodynamic analysis of the system

For the analysis of MH heat pump with EC, the thermodynamic model was developed with following assumptions:

- The EC is the only power consumer in the system, power consumed by other parts such as pumps and fans of heat exchangers are neglected.
- Enthalpy of formation (AH) and entropy of formation (AS) of MH do not change with temperature.
Metal hydride packing in the reactor is homogeneous, meaning there is no spatial distribution of temperature, and hydrogen concentration in the hydride packing is uniform.

Modeling is based on system at steady state. Proton transfer across the membrane is only dependent on current density.

Back diffusion of hydrogen across the membrane is not considered due to non-significant pressure gradient.

Electronic resistance on current collectors is neglected because it is very small (Barbir, 2005). Therefore, total cell internal resistance only accounts for membrane ionic and contact resistance.

The relationship between the midpoint of plateau pressure and temperature can be expressed with Van’t Hoff’s equation (eq. (4)).

\[
P_m = \exp \left( \frac{\Delta H}{RT} - \frac{\Delta S}{R} \right)
\]

Desorption pressure is calculated by taking into account the plateau slope and hysteresis as shown in eqs. (5)–(7).

---

Fig. 6 – Schematic diagram of EC system; Stage 1: bed 1 cooling, bed 2 heating; Stage 2: regeneration, bed 1 heating, bed 2 cooling; Stage 3: bed 1 heating, bed 2 cooling.
\[
\ln \left( \frac{P_a}{P_d} \right)_T = -\Delta P_a - \Delta P_d - \left( \frac{C}{C_{eq}} \right) - \left( \frac{P_1}{P_2} \right)_{th}
\]

(5)

\[
\ln \left( \frac{P_a}{P_d} \right)_T = -\Delta P_a - \Delta P_d - \left( \frac{C}{C_{eq}} \right) + \ln \left( \frac{P_1}{P_2} \right)_{th}
\]

(6)

\[
f_s = \ln \frac{P - \ln P_{eq}}{C - C_{eq}}
\]

(7)

where \( P_a \) and \( P_d \) are the pressures of desorption (cooling) and absorption (heating), \( f_s \) is the plateau slope factor and \( C - C_{eq} \) is the change of hydrogen content in the alloy.

For characterization of the MH, the pressure at the midpoint of the plateau is taken without considering the plateau slope \( \text{(Hirscher, 2010)} \).

\[
\frac{\Delta G_{\text{hyd}}}{RT} = \ln \left( \frac{P_a}{P_d} \right)_T
\]

(8)

where \( P_a \) and \( P_d \) are the absorption and desorption pressures at the given temperature.

The EC suction and discharge pressure are calculated in eqs. (9) and (10) based on absorption and desorption pressures plus the pressure drop between desorption reactor and EC inlet as well as absorption tank and EC outlet.

\[
P_{suc} = P_e - \Delta P_{suc}
\]

(9)

\[
P_{dis} = P_e + \Delta P_{dis}
\]

(10)

The MH desorption and absorption temperatures are calculated in eqs. (11) and (12) based on cooling and heating temperatures as well as the temperature differences for heat transfer between the reactors and surrounding.

\[
T_d = T_e - \Delta T_d
\]

(11)

\[
T_e = T_h + \Delta T_e
\]

(12)

The amount of MH required for the system is calculated in eq. (13) based on the cylindrical reactor volume.

\[
m_{\text{MH}} = \pi r_1^2 * H_b * \nu_r * \rho_{\text{MH}}
\]

(13)

where \( r_1 \) is the reactor inner radius, \( H_b \) is the reactor length, \( \nu_r \) stands for the percentage of reactor volume occupied by MH packing.

The metal hydride and metal hydride container must be sensibly cooled during refrigeration process, and sensibly heated during regeneration process, therefore, this parasitic loss needs to be considered. The entire cooling cycle includes desorption time, sensible cooling down time and regeneration time as in eq. (14).

\[
T_{\text{cycle}} = T_d + T_{\text{cd}} + T_{\text{rg}}
\]

(14)

Desorption time is calculated in eq. (15) from the amount of hydrogen stored in the MH packing, and the rate of hydrogen flowing out of container. The storage capacity of LaNi5 is taken to be 1.5% by weight \( \text{(Sandrock, 1999)} \).

\[
t_d = \frac{m_{\text{MH}} * 1.5\%}{\frac{dn}{dt} * 2}
\]

(15)

The sensible cooling down time \( (t_{\text{cd}}) \) for MH packing and the reactor is found in eq. (16) based on the enthalpy of desorption and hydrogen flow rate.

\[
t_{\text{cd}} = \frac{(C_{\text{MH}} * m_{\text{MH}} + C_h * \rho_a) \Delta T_{\text{cd}}}{\Delta H_d * \frac{dn}{dt}}
\]

(16)

where \( \Delta T_{\text{cd}} \) stands for the cooling down temperature.
The regeneration time can be found in eq. (17) based on the convection heat transfer between the reactor and the ambient.

$$t_{rg} = \frac{(C_{mat} \cdot m_{mat} + C_{w} \cdot m_{w}) \cdot \Delta T_{rg}}{h_{x} \cdot A_{x} \cdot \Delta T_{rg}}$$

where $h_{x}$ stands for the cylinder convection heat transfer coefficient, it is calculated in eq. (18) based on the Zhukauskas relation for flow over cylindrical surface (Incropera and Dewitt, 2002). $\Delta T_{rg}$ stands for the temperature change due to regeneration. $A_{x}$ stands for the surface area of the reactor.

$$h_{x} = \frac{k}{D} \cdot \frac{k}{D} \cdot C \cdot R \cdot r \cdot \left( \frac{P_{r}}{P_{r_{s}}} \right)^{\frac{1}{2}}$$

where $Nu$ is the Nusselt number, $D$ is the outer diameter of the reactor, $k$ is the air thermal conductivity, $Re$ is Reynold’s number, $Pr$ is the Prandtl number.

During the regeneration process, both hot and cold metal hydride reactors are either pre-cooled or pre-heated by air at room temperature until thermal equilibrium has been reached. Therefore, the cooling power is calculated in eq. (19) by taking the average of total cooling energy generated in terms of cooling cycle time.

$$\overline{Q}_{c} = \frac{\Delta H_{f} \cdot \frac{dn}{dt} \cdot t \cdot h_{x_{eff}}}{t_{cycle}}$$

where $h_{x_{eff}}$ is the heat exchanger effectiveness.

The heating power is calculated in the similar manner, as well as considering the time for heating up the metal hydride and the metal hydride container, and the regeneration time.

For modeling the EC, the total cell voltage of EC is expressed in eq. (20).

$$U = U_{Nernst} + U_{shm} + U_{ac}$$

where $U_{Nernst}$ stands for the Nernst potential, $U_{shm}$ is the ohmic loss of the cell due to total cell internal resistance, $U_{ac}$ stands for the anode and cathode polarization. For EC, since there is no oxygen which reacts on the cathode side to produce water, the cathode and anode polarization are very small and can therefore be neglected (Onda et al., 2007; Strobel et al., 2002). Thus the above equation is reduced to eq. (21).

$$U = U_{Nernst} + U_{shm}$$

$U_{Nernst}$ can be calculated in eq. (22) from the Nernst equation.

$$U_{Nernst} = \frac{R_{T} \cdot \ln \left( \frac{P_{\text{dis}}}{P_{\text{fue}}} \right)}{2F}$$

$U_{shm}$ of a single EC satisfies Ohm’s law (Barbir, 2005) as shown in eq. (23).

$$U_{shm} = I_{d} \cdot R_{i} = \frac{1}{N \cdot A} \cdot R_{i}$$

where $I_{d}$ is the current density of a single EC, $I$ is the total current generated by the power supply, $N$ is the number of ECs connected in parallel, $A$ is the active cell area. A typical value for $R_{i}$ depending on the thickness of Nafion membrane, is between 0.05 and 0.2 $\Omega \cdot cm^{2}$ (Barbir, 2005; Mehta and Cooper, 2002). The lower side value of 0.05 $\Omega \cdot cm^{2}$ is taken for Nafion 115 membrane with 125 $\mu$m thickness. The total power required for the EC is calculated in eq. (24) by multiplying the total cell voltage by the total current.

$$W_{EC} = (U_{shm} + U_{Nernst}) \cdot I$$

The electrochemical compression efficiency is the ratio between Nernst power ($W_{Nernst}$) and total power input required for the MEA ($W_{EC}$), based on the analogy of PEM fuel cell power efficiency (Barbir, 2005) as shown in eq. (25).

$$\eta_{EC} = \frac{W_{Nernst}}{W_{EC}}$$

which is further reduced to the ratio of Nernst potential and total cell voltage as in eq. (27):

$$\eta_{EC} = \frac{U_{Nernst} \cdot 1}{(U_{shm} + U_{Nernst}) \cdot 1}$$

The similar calculation for EC efficiency is also developed by Wong et al. (2004).

The EC power is calculated in eq. (28) based on the total amount of energy required divided by the cooling cycle time.

$$W_{EC} \cdot t_{cycle} = (U_{shm} + U_{Nernst}) \cdot I \cdot \frac{t_{cycle}}{t_{cycle}}$$

The cooling COP of system can therefore be calculated as in eq. (29).

$$\text{COP} = \frac{\overline{Q}_{c}}{W_{EC}}$$

4. Simulation results and discussion

The hydrogen flow rate across the membrane is only related to the current density for steady state analysis. Therefore, the current density can be treated in analogy to hydrogen flow rate across the membrane. Table 3 lists all the design parameters for the steady state simulation. The cross sectional area of 100 cm$^{2}$ was chosen for the EC based on the experimental work done by Rohland et al. (1998). The membrane resistance was

$$R_{i} = \frac{1}{N \cdot A} \cdot R_{i}$$
taken assuming thinner membrane is selected for the EC based on the available resistance values. The metal hydride enthalpy of formation and entropy of formation were both taken from existing measurement (Sandrock, 1999). The EC operating temperature was chosen according to Moton et al. (2014). The effects of current density, mass ratio between MH and reactor, suction and discharge pressure drop, desorption and absorption temperature drop were studied by keeping other parameters constant at 10 K for $\Delta T_{d}$, 10 K for $\Delta T_{a}$, 0.2 for $\Delta P_{dis}/P_{dis}$, 0.1 for $\Delta P_{suc}/P_{suc}$, 1.9 for $R_{m}$, 0.05 A·cm$^{-2}$ for current density, 20 for number of ECs in parallel. Some parameters were selected based on research done by Bedback and Gopal (2004) on compressor driven metal hydride heat pump. Other physical properties for LaNi$_5$ MH and its reactor were taken from the study done by Hopkins and Kim (2010), and are listed in Table 4.

Fig. 8 shows the effects of current density on system performance at constant mass ratio between MH and reactor. The cooling power increases with current density because the hydrogen flow rate increases. Meanwhile, the COP decreases. This is due to the increased ohmic loss on the EC unit, and it continuously plays a role on decreasing the compression efficiency of EC, therefore decreases the COP of the system (Fig. 9).

Fig. 10 provides the modeling results of the mass ratio between MH and reactor in terms of system performance by fixing current density. As the mass ratio $R_{m}$ increases, the cooling power increases. However, the parasitic loss also increases as more cooling energy is consumed on cooling down the increased MH mass, diminishing return is observed after $R_{m}$ value of greater than 0.8. After that, the cooling power has no significant improvement. Therefore, there is no point to increase $R_{m}$ by keep increasing the mass of MH material in the cylindrical reactor.

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**Table 3 – Fixed design parameters for steady state simulation.**

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Symbol</th>
<th>Value</th>
<th>Units</th>
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<tbody>
<tr>
<td>Cross sectional area</td>
<td>$A$</td>
<td>100</td>
<td>cm$^2$</td>
</tr>
<tr>
<td>Membrane internal resistance</td>
<td>$R_i$</td>
<td>0.05</td>
<td>$\Omega$·cm$^2$</td>
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<tr>
<td>Number of ECs in parallel</td>
<td>$N$</td>
<td>20</td>
<td>ea</td>
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<tr>
<td>Heat of formation</td>
<td>$\Delta H$</td>
<td>30.8</td>
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<tr>
<td>Entropy of formation</td>
<td>$\Delta S$</td>
<td>0.108</td>
<td>kJ·mol$^{-1}$·K$^{-1}$</td>
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<td>Membrane operating temperature</td>
<td>$T_{EC}$</td>
<td>343</td>
<td>K</td>
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<tr>
<td>Outdoor temperature</td>
<td>$T_{h}$</td>
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<td>K</td>
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<tr>
<td>Room temperature</td>
<td>$T_{c}$</td>
<td>288</td>
<td>K</td>
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**Table 4 – Physical properties for LaNi$_5$ MH and its reactor.**

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Symbol</th>
<th>Value</th>
<th>Units</th>
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<tr>
<td>Thermal conductivity</td>
<td>$k$</td>
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<tr>
<td>Specific heat</td>
<td>$C_{MH}$</td>
<td>440</td>
<td>J·kg$^{-1}$·K$^{-1}$</td>
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<tr>
<td>Density</td>
<td>$\rho_{MH}$</td>
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<td>kg·m$^{-3}$</td>
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<td>Reactor inner radius</td>
<td>$r_1$</td>
<td>0.006</td>
<td>m</td>
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<tr>
<td>Reactor wall thickness</td>
<td>$R_{wall}$</td>
<td>0.001</td>
<td>m</td>
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<tr>
<td>Reactor height</td>
<td>$H_R$</td>
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<tr>
<td>Reactor density</td>
<td>$\rho_{R}$</td>
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<td>kg·m$^{-3}$</td>
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<tr>
<td>Reactor specific heat</td>
<td>$C_R$</td>
<td>385</td>
<td>J·kg$^{-1}$·K$^{-1}$</td>
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</tbody>
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The suction and discharge pressure drops on system performance are shown in Figs. 11 and 12. Increase of suction pressure and discharge pressure drop would increase the pressure ratio, and have a marginal effect on the system performance.

Fig. 13 shows the effect of temperature difference between desorption reactor and room temperature on system performance. The temperature difference has a negligible effect on cooling power and suction pressure. However, increase of temperature difference would decrease the system COP significantly, because lowering desorption temperature would lower the EC efficiency.

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**Fig. 8 – Effect of current density on system performance.**

**Fig. 9 – Effect of EC efficiency on system performance.**

**Fig. 10 – Cooling power vs. mass ratio.**
suction pressure, which increases the EC power consumption. Fig. 14 shows the effect of temperature difference between the absorption reactor and the heating temperature. Similar to desorption process, the temperature difference has a negligible effect on discharge pressure and heating power. The COP of the system, however, decreases significantly as the temperature difference increases. In order to determine the right suction and discharge pressure drops, the reaction kinetics of MH materials, which generates sufficient desorption and absorption rate for desired performance, has to be considered.

Fig. 15 shows the EC stack volume and cooling power in terms of number of cells the stack consists of. For scaling up the system, MEA stacks need to be connected in parallel to increase the hydrogen flow rate. The volume of EC was calculated and compared with the amount of cooling power. It can be determined that a heat pump with 100 W of cooling power and COP of 3.4, at cooling and heating temperatures of 5 °C and 45 °C and current density of 0.15 A·cm$^{-2}$, requires 70 MEAs to form a 100 × 100 × 700 mm stack. The flow rate control of EC depends on the COP, volume of EC stack and required cooling power because current density generated by external voltage is the driving force of H$_2$ transport. As shown in Fig. 8, an increase of current density increases the cooling power but reduces the COP. A decrease of current density would increase the number of cell in EC stack in order to achieve the same cooling power as compared to higher current density, therefore, it increases the manufacturing cost. Therefore, there is a balance between the initial cost and the performance, and manufacturers need to take both into consideration for scaling up the system.

The life cycle of EC system is mainly constrained by the EC itself. The EC design is very similar to PEM fuel cell. The life
cycle of PEM fuel cell includes the production of materials and emissions. Pehnt (2001) stated that the production of fuel cell stacks has unneglectable environmental impact. This mainly includes impact caused by the platinum group metal catalyst production and the material and energy consumed for flow field plate production. The emission of SO2 produced by platinum production and the material and energy consumed for flow field includes impact caused by the platinum group metal catalyst stacks has unneglectable environmental impact. This mainly

5. Conclusions

In this study, an EC driven MH heat pump was proposed and studied using thermodynamic models, and its simulation results were discussed. The LaNi5 alloy was selected as a suitable alloy for the MH reactors. The system performance was evaluated based on different parameters. The simulated results show that EC efficiency has a great impact on the system COP. For a small scale heat pump with cooling capacity less than 200 W, the EC operates more efficiently than the mechanical compressor. The EC driven MH heat pump could potentially have a higher COP than the existing MH system. And quantitative analysis shows a heat pump of 100 W cooling power with COP of 3.4 and 5 °C in this paper, in additional to experiments, transient modeling also needs to be performed for better modeling the system performance.

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